

# Dynamic Characteristics of Pulse Rate Control of a POL Converter

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**Abstract** - From the perspective of good point-of-load (POL) designs, a fast response for load-change and high power efficiency are important factors. Pulse width modulation (PWM) control is a common control method for POL. Although this control method is very simple and stable for POL, the response for sudden load change is not so fast because of its fixed frequency. However, pulse rate control (PRC) is well suited to such applications. The PRC control method and its features are described, and advantages of PRC are revealed with the some simulated and experimental results.

## I. INTRODUCTION

Recently, power management has been introduced to improve the power efficiency of Micro Processing Unit (MPUs), Field Programmable Gate Array (FPGAs) and Digital Signal Processor (DSPs). The power management system includes a full operation mode, standby, and sleep modes. The clock frequency, core voltage and/or core current are changed in each mode accordingly. As a result, the output current of the point-of-load (POL) DC-DC converters is intermittent and has a high slew rate.

A low output voltage, a large output current and a high-speed response, are required for the POL [1].

In such a condition for the control circuit, highly accurate and high-speed control demands that the tolerance of the output voltage becomes internally severe, advanced by speed-up and lowering of the voltage of the MPUs, FPGAs and DSPs [2,3]. A general control method is pulse width modulation (PWM) control. However, for PWM control, the switching frequency is fixed and in this case a delay in the frequency band region results where the change of the load is higher than the switching frequency, especially a delay in the response is caused. In the worst case, the control does not catch up and there exists a possibility that the MPUs, FPGAs and DSPs will stop. In addition, there is a problem in that the ripple of the reactor current increases after the load current increases, as given by the DC bias current characteristics.

This study reveals the problem of PWM control of a POL converter, and proposes the use of pulse rate control (PRC).

PRC consists of a monostable multivibrator and an analog comparator. Switching can be immediately turned on for a change in the load, and a fast-speed response can be achieved. The change of the switching frequency causes suppression of an increase in the ripple of the reactor current.

Firstly, the basic circuitry and problems of PWM control are explained. Then a basic circuitry and the basic principle of operation regarding the PRC method are explained. In addition, the relation between the DC bias current characteristics, the ripple of the reactor current, and the effectiveness of the dynamic characteristic of the PRC method are revealed.

The results of a computer simulation are given regarding the response to a change of output voltage and ripple of the reactor current using circuit simulator Ansoft Simplorer. The experimental results are similarly shown.

## II. PWM CONTROL

Fig. 1 shows PWM control of a POL converter, where L is the choke inductor and  $C_{CO}$  is the output capacitor.  $R_{CO}$  and  $L_{CO}$  are the equivalent series resistance and the reactor of  $C_{CO}$ , respectively. In basic operation, the gate-pulse of  $SW_1$  and  $SW_2$  is output from a comparator with inputs of a triangular waveform and  $V_{err}$ .  $V_{err}$  is determined from the output voltage  $e_o$ , and a target voltage  $V_{ref}$ , through differential amplification with phase compensation.

Fig. 2 shows waveforms at load-change from light load to heavy load. The delay in the response is caused because the switching frequency is fixed for the PWM control method. To achieve a high-speed response for large load changes, speeding-up of the switching speed and addition of phases for multi-phasing are the general methods [4]. However, large switching losses and circuit size become problematic.

The output voltage  $e_o$ , is calculated as

$$e_o = \frac{T_{on}}{T_{on} + T_{off}} E_i \quad (1)$$

where  $E_i$  is the input voltage, and  $T_{on}$  and  $T_{off}$  are on and off terms.

The delay time  $t_d$ , shown in Fig. 2, is determined by

$$\frac{(1-D)}{2f_s} < t_d < \frac{(1-D)}{f_s} \quad (2)$$

where D is the duty ratio and  $f_s$  is the switching frequency. From Eq. (2), it is apparent that  $t_d$  always exists in PWM control.

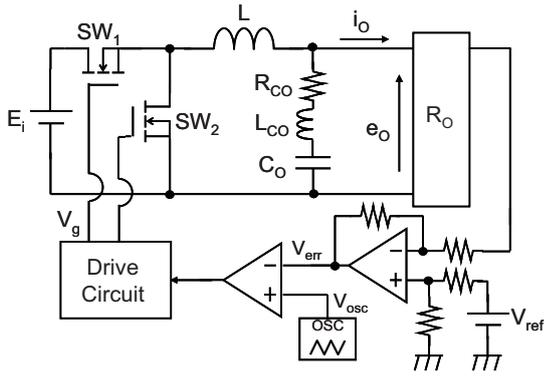


Fig. 1. PWM-controlled POL converter

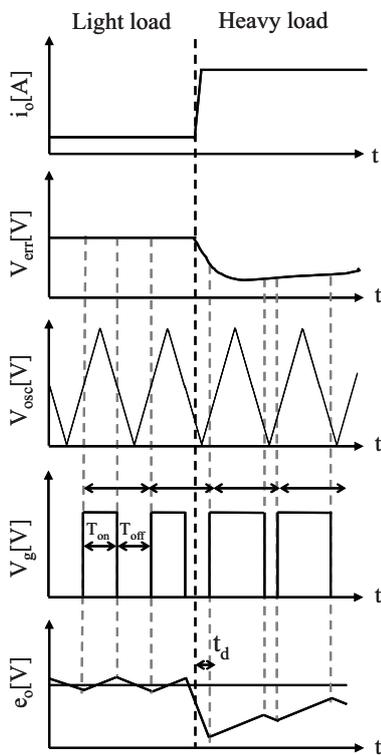


Fig. 2. Load-change from light load to heavy load.

### III. PROPOSED CONTROL CIRCUIT

#### A. Basic Operation

Fig. 3 shows the proposed PRC control circuit for the POL converter, where  $L$  is the choke inductor and  $C_O$  is the output capacitor.  $R_{CO}$  and  $L_{CO}$  are equivalent series resistance and reactor of  $C_O$ , respectively. The control block is basically composed of a comparator and a monostable multivibrator.  $V_{ref}$  is set slightly below a target output voltage  $E_o$ .

The comparator outputs a high-level signal just after the  $e_o$  dips from  $V_{ref}$ . The monostable multivibrator then outputs a pulse signal after receiving the high-level signal. The high-level signal of the monostable multivibrator continues to pre-set the term as a fixed on-term of the high-side switch  $SW_1$ . The term between the end of the on-term and the start of the

next high-level output of the comparator is the off-term of the high-side switch  $SW_1$ . Therefore, this control method can respond to load changes faster than a PWM response, especially a change from a light load to a heavy load.

$T_{on}$  for PRC is constant, and  $T_{off}$  is determined as

$$T_{off} = \frac{2L \cdot \Delta e_o}{(\Delta e_o + 2V_{ref}) \cdot R_{CO}} \quad (3)$$

where  $\Delta e_o$  is the ripple voltage of  $e_o$ .

From Eqs. (1) and (3), the following is derived

$$e_o = \frac{T_{on}}{T_{on} + \frac{2L \cdot \Delta e_o}{(\Delta e_o + 2V_{ref}) \cdot R_{CO}}} E_i \quad (4)$$

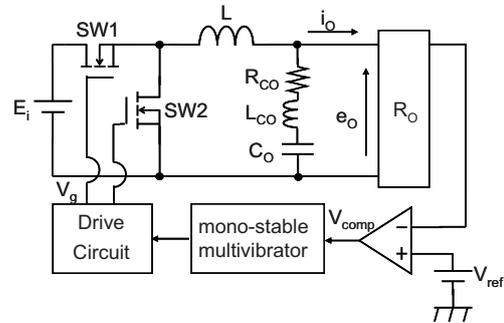


Fig. 3. Proposed PRC POL converter

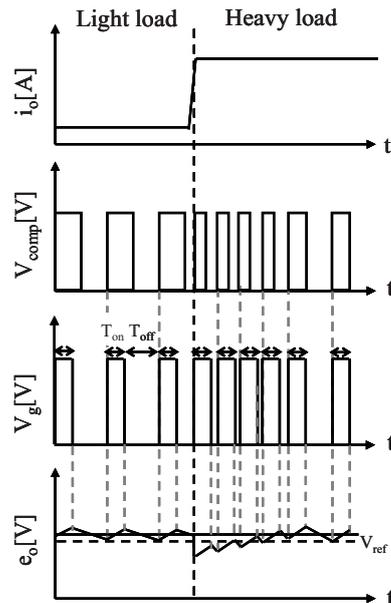


Fig. 4. Load-change from light load to heavy load

B. Suppression of the Ripple of Reactor Current

The requirements for a good choke-coil of a power supply circuit are low core-loss, miniaturization, and excellent DC bias current characteristics, etc.

However, these requirements become mutual trade-offs. Miniaturization deteriorates the DC bias current characteristics. This is especially a serious problem for control when the load-change is large, as shown in Fig. 4.

The DC bias current characteristics of a ferrite core are more excellent than those of a dust core. In any case, the inductance changes if the range of the change of direct current broadens.

The ripple of the reactor current  $\Delta i_L$ , is defined as

$$\Delta i_L = \frac{E_o \cdot (E_i - E_o)}{L \cdot f_s \cdot E_i} E_i \quad (5)$$

From Eq. (5), the value of  $E_i$ ,  $E_o$  and  $f_s$  are constant for PWM control. When the load current increases, the inductance  $L$  is decreased by the DC bias current characteristic shown in Fig. 5. As a result, the ripple of the reactor current is increased.

On the other hand, the switching frequency is not fixed in the PRC method. When the load current increases, the switching frequency increases, too. This is evident from the relation between  $I_o$  and  $f_s$ .

$$f_s = \left( 1 + \frac{R_{co} I_o}{E_o} \right) \cdot \frac{E_o}{E_i} \cdot \frac{1}{T_{on}} \quad (6)$$

Fig. 6 shows the  $I_o$ - $f_s$  characteristics under the conditions of  $T_{on}=0.5 \mu s$ ,  $E_o=1.5 V$ ,  $R_{CO}=0.05 \Omega$ .

Therefore, even if a large load change occurs from a light load to a heavy load, an increase of ripple can be decreased by the switching frequency increase, more than that by PWM control.

As a result, PRC control can improve the problem of DC bias current characteristics. It is also proposed that a low-cost dust core can be adopted as a reactor.

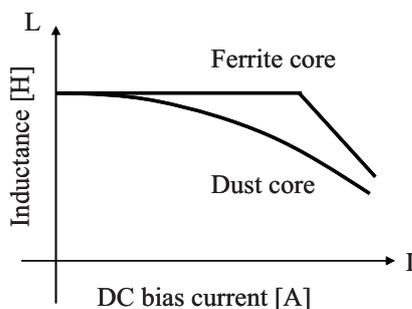


Fig. 5. DC bias current characteristics

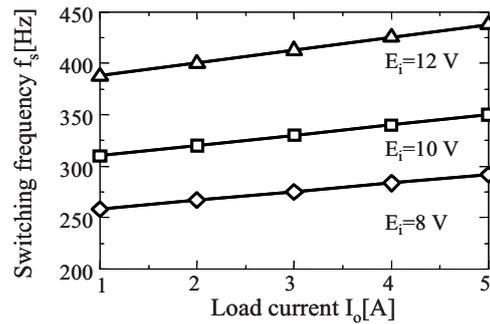


Fig. 6.  $I_o$ - $f_s$  characteristics

IV. SIMULATION RESULTS

The computer simulation analysis for PWM and PRC control were performed with a circuit simulator Ansoft Simplorer. Table 1 and 2 give the parameters and conditions used.

A. PWM Control

Fig. 7 shows waveforms for  $e_o$ ,  $i_L$  and  $v_g$  at the change point from light load to heavy load.

From the results of PWM control, a response time of 170  $\mu s$  was confirmed, with an undershoot of 69 mV and an overshoot of 25 mV. The percentage of the output voltage ripple is 1.56%. The ripple of the reactor current is 0.98 A at light load, and 1.02 A at heavy load. Therefore, the ripple of the reactor current increases by approximately 40 mA. The switching frequency is fixed at 500 kHz, and the on-term increases to step up the output voltage in the load change.

Fig. 8 shows waveforms for  $e_o$ ,  $i_L$  and  $v_g$  at the change point from heavy load to light load.

From the results of PWM control, a response time of 150  $\mu s$  was confirmed, with an undershoot of 25 mV, and an overshoot of 70 mV. The switching frequency is fixed at 500 kHz, and the on-term decreases to step down the output voltage in the load change

Table I. PARAMETERS AND CONDITIONS FOR THE SIMULATION.

Input voltage $E_i$	12V
Output voltage $e_o$	1.5V
Switching frequency $f_s$	500kHz
Choke inductor $L$	2.7 $\mu$ F
Output capacitor $C_o$	400 $\mu$ F
Equivalent series resistance $R_{CO}$	20m $\Omega$
Equivalent series reactor $L_{CO}$	1nH
Load current $i_o$ (light load-heavy load)	1A-3A
Load change slew-rate(SR)	50A/ $\mu$ s

Table II. CONTROL PARAMETERS. (SIMULATION TIME STEP:0.001 $\mu$ s)

PWM control method	
Proportional gain $H_p$	10
Integral gain $H_i$	150000
PRC method	
On-term $T_{ON}$	0.25 $\mu$ s
Minimum Off-term $T_{OFF}$	0.75 $\mu$ s
$V_{ref}$	1.49V

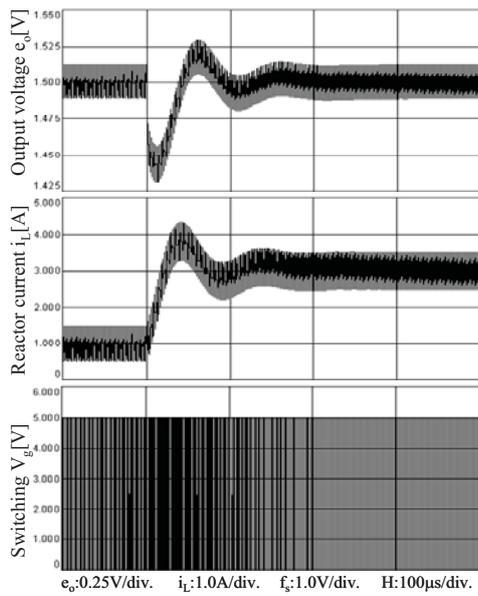


Fig. 7. Load-change simulation results from light load to heavy load (PWM control).

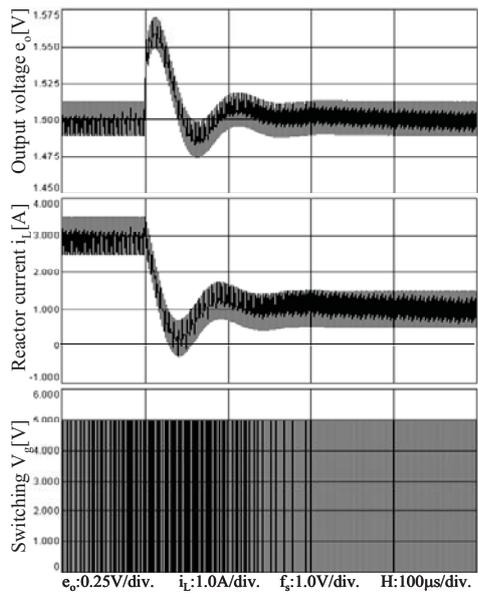


Fig. 8. Load-change simulation results from heavy load to light load (PWM control).

**B. Proposed PRC Control**

Fig. 9 shows waveforms for  $e_o$ ,  $i_L$  and  $v_g$  at the change point from light load to heavy load.

From the results of PRC, a response time of  $4 \mu s$  was confirmed, with an undershoot of  $35 mV$ . The percentage of the output voltage ripple is  $1.53\%$ . The ripple of the reactor current is  $0.982 A$  at light load, and  $0.965 A$  at heavy load. Therefore, the ripple of the reactor current decreases by approximately  $17 mA$ . The switching frequency is  $500, 530 kHz$  and  $1 MHz$  at light load, during transition, and at heavy

load, respectively. When the load current increases, it was confirmed that the switching frequency also increases.

Fig. 10 shows waveforms for  $e_o$ ,  $i_L$  and  $v_g$  at the change point from heavy load to light load. From the results of PRC, the response time was confirmed as  $5 \mu s$ , with an overshoot is  $35 mV$ . The switching waveform was kept off-term during transition, until the output voltage decreased to the target output voltage.

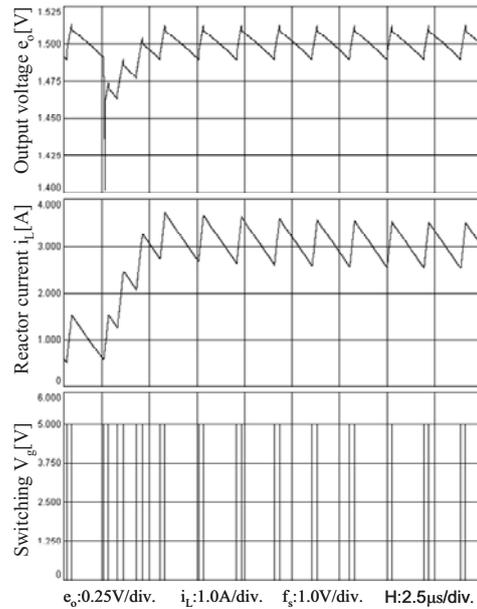


Fig. 9. Load-change simulation results from light load to heavy load (PRC).

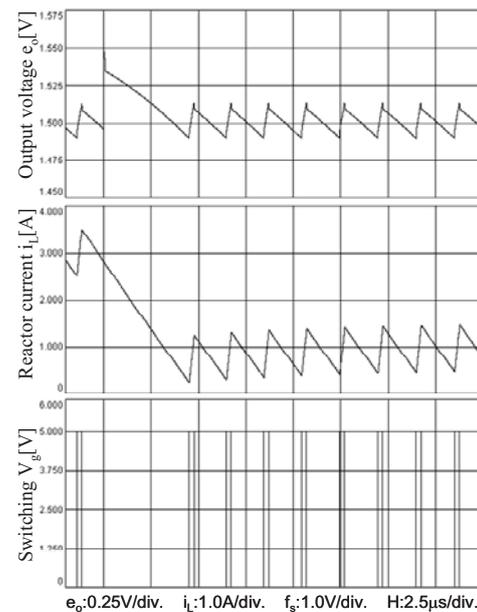


Fig. 10. Load-change simulation results from heavy load to light load (PRC).

V. EXPERIMENTAL RESULTS

A. PWM Control

The experiments were performed using a PWM control-IC (TPS40050, Texas Instruments Co.) [5].

Fig. 11 shows the experimental circuit, and Table 3 gives the experimental conditions.

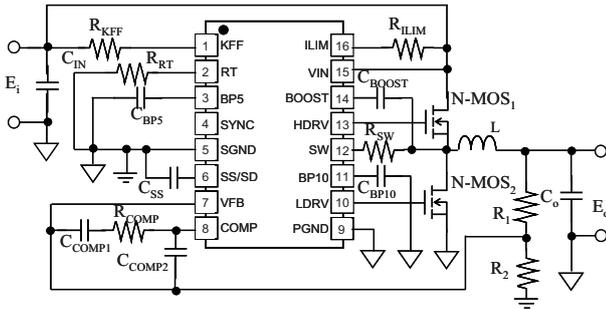


Fig. 11. Experimental circuit (PWM).

Table III.

EXPERIMENTAL CONDITIONS.			
Input voltage $E_i$	8V	Load current $i_o$ (light load-heavy load)	0.6A-1.4A
Output voltage $E_o$	4V		
Switching frequency $f_s$	500kHz	Choke inductor L	2.7 $\mu$ F
$C_{BOOST}$	0.1 $\mu$ F	Output capacitor $C_o$	330 $\mu$ F
$R_{KFF}$	30k $\Omega$	Input capacitor $C_{in}$	20 $\mu$ F
$R_{SW}$	3.3k $\Omega$	$R_1$	100k $\Omega$
$R_{RT}$	90k $\Omega$	$R_2$	13.2k $\Omega$
$R_{ILIM}$	3.09k $\Omega$	$C_{BP10}$	1 $\mu$ F
$C_{BP5}$	0.1 $\mu$ F	$C_{SS}$	3300pF
$C_{COMP1}$	1000pF	$C_{COMP2}$	82pF

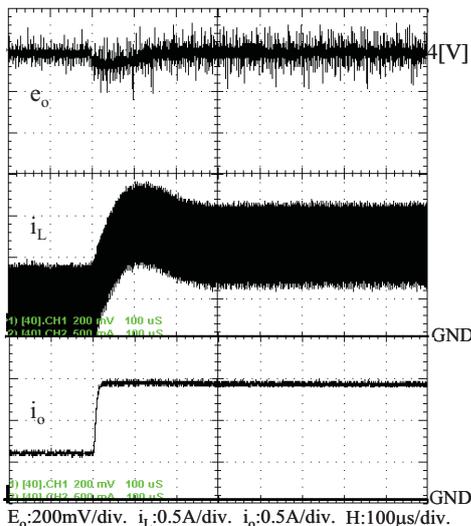


Fig. 12. Load-change experimental results from light load to heavy load (PWM control).

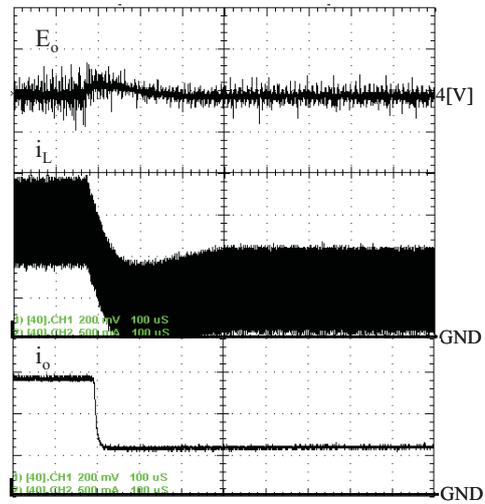


Fig. 13. Load-change experimental results from heavy load to light load (PWM control).

Fig. 12 shows waveforms for  $e_o$ ,  $i_L$  and  $i_o$  at the change point from light load to heavy load.

From the results of PWM control, it was confirmed that the response time is 150  $\mu$ s, with an undershoot of 80 mV. The ripple of the reactor current is 0.95 A at light load, and 0.97 A at heavy load. Therefore, the ripple of the reactor current increases by approximately 20 mA. Also, the noise of the output voltage was greater for the heavy load than for the light load. The switching frequency was fixed at 500 kHz, and the on-term increases to step up the output voltage in the load change.

Fig. 13 shows waveforms for  $e_o$ ,  $i_L$  and  $i_o$  at the change point from heavy load to light load.

From the results of PWM control, it was confirmed that the response time is 200  $\mu$ s, with an overshoot of 60 mV. The switching frequency was fixed at 500 kHz, and the on-term decreases to step down the output voltage in the load change.

B. Proposed PRC

The experiments were performed using a PRC-IC (SI-8405N, Sanken Electric Co., Ltd.) [6].

Fig. 14 shows the experimental circuit, and Table 4 gives the experimental conditions.

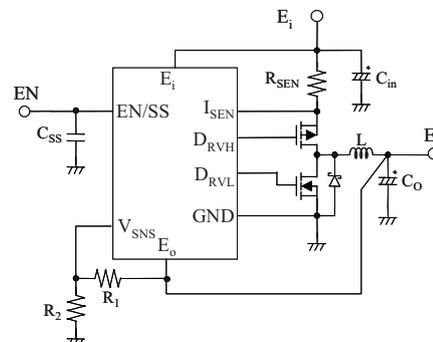


Fig. 14. Experimental circuit (PRC)

Table IV.

EXPERIMENTAL CONDITIONS.			
Input voltage $E_i$	5V	Load current $i_o$ (light load-heavy load)	0A-1.4A
Output voltage $E_o$	2.5V	Choke inductor L	2.7 $\mu$ F
Switching frequency $f_s$	500kHz	Output capacitor $C_o$	330 $\mu$ F
On-term $T_{ON}$	1 $\mu$ s	Input capacitor $C_{in}$	20 $\mu$ F
soft-start capacitor $C_{ss}$	0.022 $\mu$ F	MOS Pch/Nch 1PkgSOP8(Toshiba)	

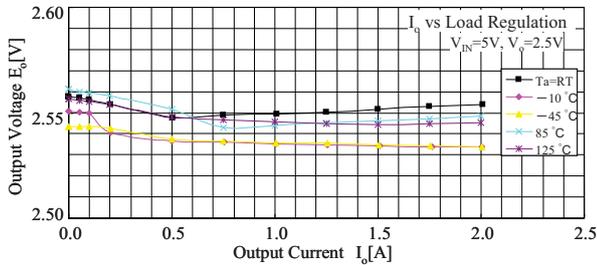


Fig. 15.  $I_o$ - $E_o$  characteristic.

Fig. 15 shows the  $I_o$ - $E_o$  characteristics for various temperatures. The error is a maximum of 0.02 V for the temperature change. The error rate with a standard voltage is within 2%. Therefore, it was confirmed that highly accurate control is achieved.

Fig. 16 shows waveforms for  $e_o$ ,  $i_L$  and  $i_o$  at the change point from light load to heavy load. From the results of PRC, it was confirmed that the response time is 6  $\mu$ s, with an undershoot of 20 mV. The ripple of the reactor current is 0.77 A at light load, and 0.62 A at heavy load. Therefore, the ripple of the reactor current decreases by approximately 150 mA. The switching frequency is 500, 620 and 830 kHz at light load, during transition and at heavy load, respectively. When the load current increases, it was confirmed that the switching frequency also increases.

Fig. 17 shows waveforms for  $e_o$ ,  $i_L$  and  $v_g$  at the change point from heavy load to light load. From the results of PRC, it was confirmed that the response time is 4  $\mu$ s, with an overshoot of 40 mV. The switching waveform is kept as an off-term during transition, until the output voltage falls to the target output voltage.

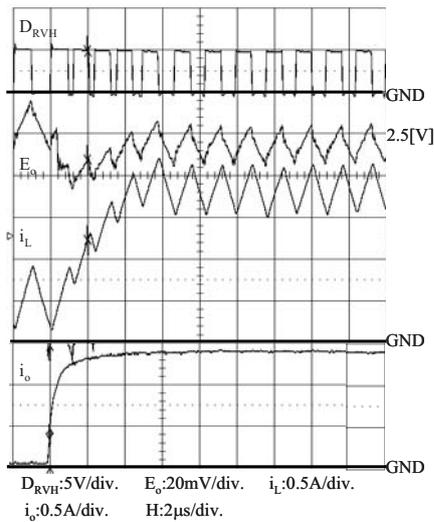


Fig. 16. Load-change experimental results from light load to heavy load (PRC).

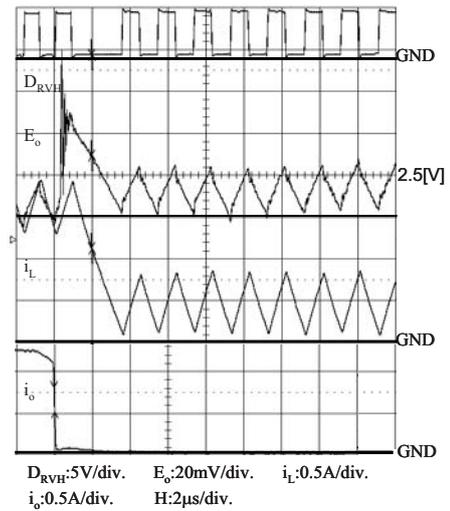


Fig. 17. Load-change experimental results from heavy load to light load (PRC).

VI. CONCLUSION

PWM and PRC control were compared from the aspect of dynamic characteristics using a simulation and experiments. The results gained from PRC suggest that the response time was decreased dramatically. These results indicate that PRC not only allows fast response but also fast convergence. In addition,  $\Delta i_L$  decreased after the load change. This suggests that the increase in the switching frequency cancelled out the influence of the DC bias. The switching frequency was 500, 620 and 830 kHz at light load, during transition and at heavy load, respectively.

ACKNOWLEDGEMENT

This work was supported in part by the Grant-in-Aid for Scientific Research (No.16560246) of Japan Society for the Promotion of Science and the Ministry of Education, Science, Sports and Culture.

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