# Density Measurements of Poly(Acrylic Acid) Potassium Salts

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Density measurements of poly(acrylic acid) potassium salts (PAK) with different degrees of neutralization and water contents are presented. apparent partial molar volumes of polymer, V2, and the partial molar volumes of water, V<sub>1</sub>, were calculated from the densities. The values of V<sup>\*</sup><sub>2</sub> decreased with increasing water content and eventually leveled off. values of V<sub>1</sub>, which at low water contents were much smaller than that of free water, increased with increasing water content and reached that of free water, showing consequently the appearance of free water. the final value of free water, the data indicated the formation of primary and secondary hydration shells. The structure of primary hydration was suggested to be of body-centered cubic coordination in which carboxyl oxygen atoms participate.

#### Introduction

During the course of an investigation of the physical properties of poly (acrylic acid) salts in solid state, it became desirable to have the information for the hydrated state of ionic sites. In the preceding studies1,2,3 on drying process and equilibrium water uptake of poly (acrylic acid) (PAA), its sodium salts (PANa), potassium (PAK), and lithium salts (PALi), it became apparent that there are critical extents of neutralization for the additivity between epuilibrium water uptake and the extent of neutralization. From these unusual behaviors of hydration of PAA salts, it seemed reasonable to assume that the appearance of the vacant coordination sites of metal atoms play an important role in the hydration of PAA salts. The state of hydrated water molecules was studied by pulsed n.m.r. technique for PALi, PANa, and PAK4) and by partial molar volume for PANa<sup>5)</sup>.

The object of this work is to study the hydration of the completely and partially neutralized PAK in further detail through the measurement of partial molar volume. Although the literature contains a number of references to the investigation of partial molar volume of PAA salts<sup>6,7)</sup>, the studies have not been extended beyond very dilute solutions. Contrary, the work described below deals with the state ranging from solid

Received October 15th, 1982

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to highly concentrated solutions. The data showed that there are different stages of hydration with increasing water content.

## Experiment

Preparation of PAK with degrees of neutralization varying from 0 to 100 % were described in the preceding paper<sup>1)</sup>. The degree of neutralization will be denoted by the numbers added to the abbreviated name as illustrated by PAK 30. The densities of the samples with different water contents were measured with a  $25 \text{ cm}^3$  Harvard type pycnometer at  $25^{\circ}\text{C}$ . After preliminary examinations, p-xylene was chosen as the medium for density measurements because of its relatively low volatility and inactivity to samples. p-Xylene was distilled under reduced pressure.

## Results

The densities of PAK with different water contents are shown in Fig. 1. The values of density decreased with increasing water content and increased with increasing degree of neutralization. In the following calculations, polymer mol refers to the repeat unit mol. Apparent partial molar volumes of PAK,  $V_2^*$ , were calculated from

$$\rho = \rho_1^0 + (1 - \rho_1^0 / \rho_2^*) c_2$$
 (1)

$$V_{\bullet}^{*} = M/\rho_{\bullet}^{*} \tag{2}$$

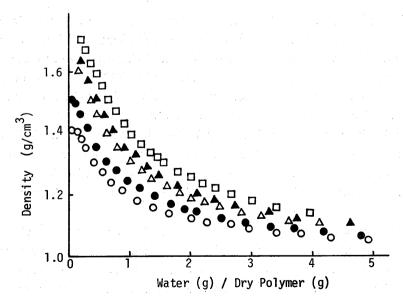


Fig. 1 Densities of poly (acrylic acid) potassium salts with degrees of neutralization from 0 to 100% at 25°C; neutralization%, 100% □, 60% ▲, 45% △, 15% ●, 0% ○.

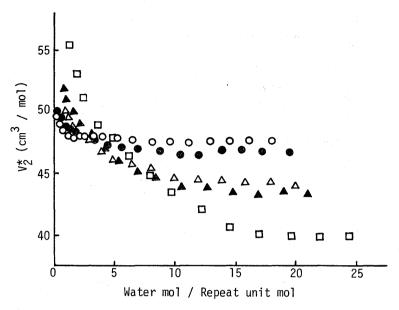


Fig. 2 Apparent molar volumes of poly(acrylic acid) potassium salts with degrees of neutralization from 0 to 100% at 25°C; neutralization %, 100%  $\square$ , 60%  $\blacktriangle$ , 45%  $\triangle$ , 15%  $\bigcirc$ , 0%  $\bigcirc$ .

where  $\rho$  is the density of sample,  $\rho_1^o$  density of the water at 25°C (0.99705 g/cm³),  $c_2$  polymer concentration in g per 1 cm³ of solution, M the number average molecular weight of the repeat unit. The calculated values of  $V_2^*$  of PAK are plotted as a function of water content in Fig. 2. The values of  $V_2^*$  decreased with increasing the degree of neutralization.

For the determination of the partial molar volumes of water and polymer, mean molar volume of the solution  $V_m$  are introduced, as defined by Eqs. (3) and (4),

$$V_m = V/(n_1 + n_2)$$
 (3)

$$V_{m} = X_{2} (dV_{m}/dX_{2}) + V_{i}$$
(4)

where V is the sample volume,  $n_1$  and  $n_2$  are the numbers of moles of water and polymer, respectively, and  $X_2$  the mole fraction of polymer. Partial molar volumes of water and polymer,  $V_1$ , and  $V_2$ , can be determined from the intercepts of the tangent to the curve of  $V_m$  against  $X_2$ . The values of  $V_1$  are summarized in Fig. 3. The values of  $V_2$  were not determined because of the uncertainty of extrapolation to  $X_2=1$ , since the plots were limited to small values of  $X_2$  owing to the large difference of molecular weights between water and polymer (repeat unit).

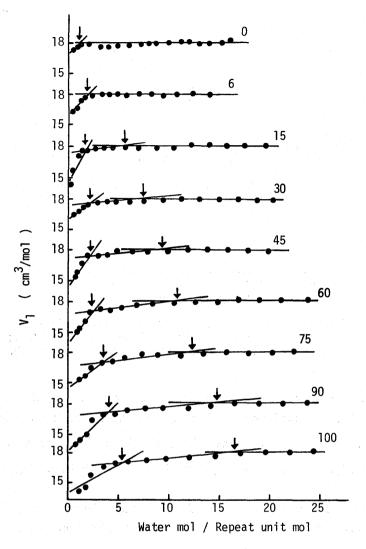


Fig 3 Molar volumes of water coexisting with poly (acrylic acid) potassium salts at 25°C. Neutralization % are indicated in the figure.

## Discussion

The partial molar volume of water,  $V_1$ , finally reached the constant value of 18 cm<sup>3</sup>/mol which is the value of free water at 25°C (18.02 cm<sup>3</sup>/mol) in the region of low mole fraction of polymer, that is, at high water contents. In this region, of course, apparent molar volumes of the polymer,  $V_2^*$ , have constant values, which should be almost equal to the partial molar volumes of polymer,  $V_2$ . As Fig. 2 shows, this value was  $48.6 \text{ cm}^3/\text{repeat}$  unit mol for PAA and decreased with increasing neutralization %. The value for PAK 100 was  $40.6 \text{ cm}^3/\text{repeat}$  unit mol. The both values are in good agreement with those reported by Ise et al.<sup>6)</sup> (47.8 and 43.0, respectively) and Tondre et al.<sup>7)</sup> (46.7 and 38.2. respectively) in the study of dilute solution. The decrease in

V<sub>2</sub> with neutralization is natural where solvation occurs in solution.

In Fig. 3, it is observed that before attaining the final value the partial molar volume of water increases as the water content increases, but a simple relationship does Though there seems to be an almost linear increase for the samples with low neutralization %, distinct bendings of the plots appear as neutralization % increases. It is reasonable to consider that the hydration mechanism is different before and after these bendings. The first portion of the plot before bending is inferred to be the direct hydration to ion pairs. In this stage the carboxyl two oxygen atoms may be coordinated to metal atom in body-centered cubic coordination which was demonstrated in our previous  $study^{2}$ . The structure is illustrated in Fig. 4. Such a chelation of carboxyl group is in line with the coordination structure of copper acetate monohydrate<sup>8)</sup>. In the case of Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> ions, though tetrahedral coordination has been verified for Li<sup>+</sup>9), Na<sup>+</sup>10), and K<sup>+11,12)</sup> ions, through the X-ray study on concentrated aqueous solution of alkali hydroxide or alkali halaide, tetrahedral coordination is impossible where chelation of carboxyl occurs, since ionic radii of Li+, Na+, and K+ are much greater than that of the internal sphere of tetrahedron formed by chelation of carboxyl oxygen atoms. vacant sites of coordination of metal atom will be occupied by oxygen atom of water molecules until the vacant sites diminished. The secondary hydration of water molecules to this primary hydration shell through coulomb interaction, and/or hydrogen bonding will continue hereafter. Further increase of water content leads to the appearance of free (bulk) water, which corresponds to the point where V1 approaches 18.02. From the above consideration we can expect that the molar ratio of water to polymer where primary hydration sites are fulfilled is 6 for PAK 100. For partially neutralized samples, the molar ratio should be smaller than 6, depending upon the degree of neutralization.

As the degree of neutralization decreases, the amount of ion pair decreases. As

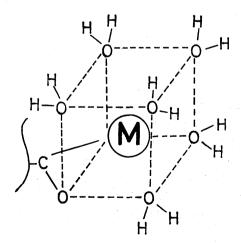


Fig. 4 A model for the body-centered cubic coordination structure of metal atom.

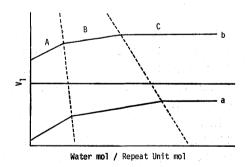


Fig. 5 The schematically represented variation of the plot of V<sub>1</sub> as a function of water content and the degree of neutralization A, primary hydration range; B, secondary hydration range; C, free water; a, high degree of neutralization; and b, low degree of neutralization.

a result, the both points where secondary hydration begins and free water appears should shift toward the smaller water content. At the same time the limiting value of  $V_1$  at low water content should increase. In consequence, the change of the slopes due to the onset of secondary hydration will become indistinct. The situation is illustrated schematically in Fig. 5.

The molar ratio of water to polymer (repeat unit mol) where free water appears (where  $V_1$  levels off to 18.02) increases with the increase of neutralization %. The ratio for completely neutralized PAK 100 is 16.5. As a simple calculation shows, the solution is still a fairly concentrated one. It is not expected that dissociation of ion pair occurs substantially in this solution. If we assume this situation, we may imagine the hydration shell of ion pair still exists at this stage. Further increase of water content should lead to the separation of ion pair and the appearance of hydration shell of cation ( $K^+$ ) and anion ( $-COO^-$ ). The separation of both ions in this stage may not contribute to the partial molar volume of water because all ions are buried in hydration shell already.

From the consideration described above it seems appropriate to regard the hydration number determined to be 16.5 as different from the hydration numbers in ordinary meaning. The latter values have been determined usually in dilute aqueous solutions where ions are in almost completely separated state. In addition, they vary according to the different characteristic of each measurement. Therefore it was avoided to compare the hydration number in this study with those for K<sup>+</sup> ion reported in a variety of studies. However, it should be emphasized here that the results in this study clarified that (1) primary hydration is saturated at very low water content, (2) then, secondary hydration followed, (3) free water appears in fairly low content of water. These conclusions help to understand the complicated behavior of ionic polymers in solid state where a trace of water strongly influence the physical properties through shielding coulomb interactions.

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